



## PRESENTACIÓN

**Breve descripción:** The objective of this course is to provide advanced elements of linear algebra, necessary for other courses in advanced mathematics and data analytics.

- **Titulación:** Grado en Economía
- **Módulo/Materia:** Módulo 3: Métodos Cuantitativos / Materia: 3.1: Métodos Cuantitativos
- **ECTS:** 3
- **Curso, semestre:** 2º course, 1st semester
- **Carácter:** Mandatory
- **Profesor:** Luis Alberiko
- **Idioma:** English

## RESULTADOS DE APRENDIZAJE (Competencias)

**Basic competences** (Module 3. Quantitative Methods):

BC3: Students must have the ability to gather and interpret relevant data (usually within their area of study) to make judgments that include a reflection on relevant social, scientific and ethical topics.

**Specific competences** (Module 3. Quantitative Methods):

SC8: To analyse quantitative information on economic and business phenomena and variables using mathematical and/or software tools.

SC15: To analyse data using software tools on specific areas of economics and/or business.

**Specific competences** (Diploma in Data Analytics):

SSOP1: Accessing and managing massive data

SSOP2: Understanding programming languages potentially used to solve economic and/or business problems

SSOP3: Working with visual elements that provide insights and an understanding into complex concepts and components of economic and/or business problems

SSOP4: Identify patterns and trends and gather useful information from massive data in economics and/or business.

SSOP5: Effective communication of results to a professional audience in economics and/or business

GC4: Reason autonomously and critically on issues relevant to economics and business.

SC5: Apply mathematical reasoning and/or quantitative tools to the analysis of economic reality.

SC6: Use software tools in the quantitative and/or qualitative analysis of economic and/or business issues with sound judgment.

SC8: Apply economic logic and/or econometric techniques to specific areas of Economics.



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## PROGRAMA

### Unit 1: Vectors and Matrices

1.1 Vectors and vector operations. Geometric interpretation in the Cartesian plane.

1.2 Linear combinations of vectors.

1.3 Basics in matrix algebra.

1.4 Matrix algebra in  $\mathbb{R}$ .

### Unit 2: Linear Transformations

2.1 The vector space

$\mathbb{R}^n$

. Vector subspaces. Linearly independent/dependent vectors.

2.2 Basis and dimension. Change of basis.

2.3 Linear transformation between vector spaces.



2.4 Matrix representation of a linear transformation. Matrix multiplication as two consecutive linear transformations.

2.5 The inverse of a linear transformation.

### **Unit 3: Eigenvalues and Eigenvectors**

3.1 Eigenvalues and eigenvectors. The characteristic equation.

3.2 Eigenbasis.

3.3 The diagonal matrix.

3.4 Matrix diagonalization.

3.5 Computing eigenvalues and eigenvectors in R.

### **Unit 4: Further Applications in Data Processing and Analysis**

4.1 Orthogonality, orthogonal/orthonormal matrices.

4.2 Collinearity and data redundancy.

4.3 The variance-covariance matrix and the correlation matrix.

4.4 Singular value decomposition. Singular value decomposition in R.

4.5 Principal component analysis. Principal component analysis in R.

## **ACTIVIDADES FORMATIVAS**

Within the formation activities the students will have to attend one econometric/statistical seminar per month. They may also participate in all the other seminars and congresses organized by the Faculty of Economics.

Clases teoricas y / o practicas: 24 horas teotricas + 6 horas practicas

Trabajos individuales y / o grupos: 50 horas

Estudio personal: 200 horas

Tutorias: 10 horas

## **EVALUACIÓN**

The final grade in this course will be a weighted average of different exams, with the weights being as follows:

### **CONVOCATORIA ORDINARIA**

- Class participation and exercises: 15%
- Final exam: 85%

### **CONVOCATORIA EXTRAORDINARIA**



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- Final exam: 100%

There will be a continuous evaluation that will be related to class participation and exercises during the course. It will take 15% of the final score.

## HORARIOS DE ATENCIÓN

Fridays, from 12.00 to 5.00pm

Online at any time

Prof. Luis Alberiko ([alana@unav.es](mailto:alana@unav.es))

## BIBLIOGRAFÍA

### Basic bibliography:

- Larson, R. (2013). *Elementary Linear Algebra*. Ed. 7th Australia: Brooks/Cole Cengage Learning. (ISBN: 9781133111344). [Find it in the library](#)
- Abadir, K. M. and Magnus, J. R. (2005). *Matrix algebra*. Cambridge University Press (ISBN: 9780521822893) [Find it in the library](#)
- Aleskerov, T and Ersel, H and Piontkovski, D. (2011). *Linear algebra for economists*. 1st edition. Springer (ISBN: 9783642205705). [Find it in the library \(ebook\)](#)

### To practice using R:

- Dayal, V (2020). *Quantitative Economics with R*. Springer (ISBN: 978-981-15-2035-8). [Library catalog link](#).

### To practice more exercises:

- Bronson, R and Costa, G. B. (2009). *Matrix methods*. 3rd edition. Elsevier (ISBN: 978-0-12-374427-2). [Library catalog link](#).

### Complementary bibliography:

- Theil, H. (2007) Chapter 1: *LINEAR ALGEBRA AND MATRIX METHODS IN ECONOMETRICS*. *Handbook of econometrics*, edited by James J. Heckman and Edward Leamer. 1st edition. North Holland (ISBN: 9780444532008). [Library catalog link](#).
- Magnus J. R. and Neudecke H. (2019). *Matrix differential calculus with applications in statistics and econometrics*. 3rd edition. John Wiley & Sons (ISBN: 9781119541202). [Library catalog link](#)